

Gains from Monetary Policy Cooperation under Dollar Pricing

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Definitions

- Producer currency pricing (**PCP**): Firms set all prices in their own currency
- Local currency pricing (**LCP**): Home (Foreign) firms set export prices in Foreign (Home) currency and domestic prices in their own currency
- Dollar pricing (**DP**): **Home** firms set all prices in their own currency (**PCP**), while **Foreign** firms set export prices in Home currency and domestic prices in their own currency (**LCP**)
 - **Under DP**, every **international trade** transaction is priced in **U.S. dollars** (Home currency)

Motivation

- Almost every international trade transaction is priced in U.S. dollars
 - Gopinath and Rigobon 2008: 90% of U.S. imports and 97% of U.S. exports are priced in U.S. dollars for the period 1994-2005
- This suggests that open economy models with symmetric export pricing, i.e. PCP models or LCP models, do not seem to be plausible
 - In symmetric export pricing models, more than one currency are used in international trade transactions

Motivation

- Dominant role of the U.S. dollar in international trade can have significant influences on the transmission of shocks across countries, and hence welfare
- Nevertheless, most studies have not considered the dominant role of the U.S. dollar in international trade
 - Almost all researchers still use two-country models with symmetric export pricing (either PCP or LCP) to study optimal monetary policy in open economies

Aim

- Construct a two-country model with asymmetric export pricing (i.e. DP model)
- Derive quadratic loss functions of cooperative and noncooperative policymakers
- Compute welfare gains from monetary policy cooperation in the DP model, and examine
 - whether welfare gains from cooperation exist
 - whether the gains are larger than those in the LCP and PCP models
 - whether Home (U.S.) gains are greater than Foreign (rest of the world) gains

Literature

- Related to the literature on optimal monetary policy in open economies and export price setting
 - PCP: Clarida, Galí and Gertler (2002), Benigno and Benigno (2006), etc.
 - LCP: Engel (2011), Fujiwara and Wang (2017), etc.

Literature

- Few studies assume DP
 - Corsetti and Pesenti (2007), Devereux, Shi and Xu (2007), Goldberg and Tille (2009): consider **one-period stochastic models** with one-period ahead price setting (and thus **fully sticky prices**)
 - Mukhin (2018): Do **not utilize the linear-quadratic framework**, do **not explicitly calculate the welfare gains**, and **focus only on cooperation**
 - Egorov and Mukhin (2020): Do not utilize the linear-quadratic framework, do not explicitly calculate the welfare gains and assume the **U.S. as a small open economy**
- ⇒ This paper is **complementary to Mukhin (2018) and Egorov and Mukhin (2020)**

Illustration

- PCP model
 - Exist the inefficiency arising from the internal relative price (P_F/P_H) misalignments
 - National CB can manipulate the internal relative price to improve its welfare through nominal exchange rate adjustment
 - Note that the internal relative price and the terms of trade are equalized under PCP since LOOP holds

⇒ Small gains from monetary policy cooperation

Illustration

- LCP model
 - Does **not exist the inefficiency** arising from the internal relative price misalignments
 - Import prices are set in local currencies → CB cannot control the price to improve welfare through nominal exchange rate adjustment
 - Do exist the **inefficiency** arising from currency misalignments (deviations from the LOOP)
 - LOOP does not hold → CB can engineer the currency misalignments to improve welfare through nominal exchange rate adjustment

⇒ Small gains from cooperation but larger than PCP model

Illustration

- DP model
 - Exist the inefficiencies arising from both the internal relative price and currency misalignments
 - LOOP partially holds. LOOP for Home goods holds but that for Foreign goods does not hold
 - Home cannot control the internal relative price, since its import prices are set in Home currency by Foreign firms
 - But Foreign can control the internal relative price through nominal exchange rate adjustment, because its import prices are set in Home currency

Illustration

- DP model
 - Since LOOP for Foreign goods does not hold, Foreign can control currency misalignments by adjusting the nominal exchange rate
 - But Home cannot, because LOOP for Home products holds

Illustration

- In the DP model, there is **one more inefficiency** compared to the PCP and LCP models
- ⇒ **Gains** from cooperation are **greater** than those in the PCP and LCP models
- **Only Foreign can control** both the **internal relative price** and **currency misalignments** through nominal exchange rate adjustment
- ⇒ **Rationalize** the fact that the **U.S. designates currency manipulators** to protect its welfare
- ⇒ **Home gains** are **larger**

Illustration

- Under **log utility**, **unitary elasticity of substitution** between Home and Foreign goods and **no home bias**, there are **no gains** from cooperation in the **PCP and LCP models**
 - In the **PCP** model **with log utility and unitary elasticity of substitution**, the **internal relative price interdependence is absent** → **no gains** from cooperation
 - In **symmetric models** such as the LCP and PCP models, the **Home internal relative price and the inverse of the Foreign internal relative price are equal** → combining this and **no home bias** generates **constant real exchange rate** → there are **no deviations from the LOOP** in the LCP model → **no gains** from cooperation

Illustration

- In the DP model, the internal relative price interdependence disappears under the conditions
 - However, there are still currency misalignments
 - Thanks to the asymmetry of the DP model, the LOOP still does not hold for Foreign products
- ⇒ There are gains from monetary policy cooperation even under the conditions

The model

Overview

- The world economy consists of **two countries**: **Home (U.S.)** and **Foreign (rest of the world)**
- Home and Foreign are **symmetric with exception of export pricing**
 - Firms in Home set all prices in their own currency, while those in Foreign set export prices in Home currency and domestic prices in their own currency
 - Hence, **only** Home currency (**U.S. dollar**) is used in **international trade**
- The population size in each country is normalized to one and asset markets are complete

Households

- Utility:

$$W_H = \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\frac{C_t^{1-\sigma}}{1-\sigma} - \chi \frac{h_t^{1+\omega}}{1+\omega} \right] \quad (1)$$

- Aggregate consumption:

$$C_t = \left\{ (1-\gamma)^{\frac{1}{\eta}} C_{H,t}^{\frac{\eta-1}{\eta}} + \gamma^{\frac{1}{\eta}} C_{F,t}^{\frac{\eta-1}{\eta}} \right\}^{\frac{\eta}{\eta-1}} \quad (2)$$

- LOOP partially holds

$$P_{H,t} = E_t P_{H,t}^*, \quad P_{F,t} \neq E_t P_{F,t}^* \quad (3)$$

Relative prices

- Home and Foreign **currency misalignment** (deviations from the LOOP):

$$m_t = \frac{E_t P_{H,t}^*}{P_{H,t}} = 1, \quad m_t^* = \frac{E_t P_{F,t}^*}{P_{F,t}} \quad (4)$$

- Home and Foreign **internal relative prices**, s_t and s_t^* :

$$s_t = \frac{P_{F,t}}{P_{H,t}}, \quad s_t^* = \frac{P_{H,t}^*}{P_{F,t}^*} \quad (5)$$

- Home and Foreign terms of trade, τ_t and τ_t^* , are

$$\tau_t = \frac{P_{F,t}}{E_t P_{H,t}^*}, \quad \tau_t^* = \frac{E_t P_{H,t}^*}{P_{F,t}} \quad (6)$$

Note that $\tau_t = s_t$ but $\tau_t^* \neq s_t^*$

Firms

- Production:

$$Y_t(j) = \exp(z_t) h_t(j) \quad (7)$$

- Firms' resource constraints:

$$Y_t(j) = C_{H,t}(j) + C_{H,t}^*(j) \quad (8)$$

Price setting and aggregate resource constraints

- Home firm j maximizes

$$\mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \theta^{t-t_0} Q_{t_0,t} [(1 + \mu) P_{H,t_0}(j) \{C_{H,t}(j) + C_{H,t}^*(j)\} - MC_t Y_t(j)] \quad (9)$$

- Foreign firm j^* maximizes

$$\mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \theta^{t-t_0} Q_{t_0,t}^* \left[(1 + \mu) \left\{ P_{F,t_0}^*(j^*) C_{F,t}^*(j^*) + \frac{P_{F,t_0}(j^*)}{E_t} C_{F,t}(j^*) \right\} - MC_t^* Y_t^*(j^*) \right] \quad (10)$$

- Aggregate resource constraints:

$$Y_t = \Delta_t C_{H,t} + \Delta_t C_{H,t}^*, \quad Y_t^* = \Delta_{F,t} C_{F,t} + \Delta_{F,t}^* C_{F,t}^* \quad (11)$$

Linear-quadratic framework

Linear constraints

- NKPCs:

$$\hat{\pi}_{H,t} = \beta \mathbb{E}_t [\hat{\pi}_{H,t+1}] + \delta \left\{ (\sigma + \omega) \hat{Y}_t - (1 + \omega) z_t - \gamma(1 - \eta\sigma) (\hat{s}_t^* - \hat{e}_t) - \gamma(1 - \eta\sigma) \hat{m}_t^* \right\} \quad (12)$$

$$\hat{\pi}_{F,t}^* = \beta \mathbb{E}_t [\hat{\pi}_{F,t+1}^*] + \delta \left\{ (\sigma + \omega) \hat{Y}_t^* - (1 + \omega) z_t^* + \gamma(1 - \eta\sigma) (\hat{s}_t^* - \hat{e}_t) - \gamma\eta\sigma \hat{m}_t^* \right\} \quad (13)$$

$$\hat{\pi}_{F,t} = \beta \mathbb{E}_t [\hat{\pi}_{F,t+1}] + \delta \left\{ (\sigma + \omega) \hat{Y}_t^* - (1 + \omega) z_t^* + \gamma(1 - \eta\sigma) (\hat{s}_t^* - \hat{e}_t) + (1 - \gamma\eta\sigma) \hat{m}_t^* \right\} \quad (14)$$

Linear constraints

$$\hat{Y}_t - \hat{Y}_t^* + \eta(1 - \gamma)\hat{\rho}_{H,t} + \eta\gamma\hat{\rho}_{H,t}^* - \frac{1 - 2\gamma}{\sigma}\hat{e}_t - \eta(1 - \gamma)\hat{\rho}_{F,t}^* - \eta\gamma\hat{\rho}_{F,t} = 0 \quad (15)$$

$$\hat{\pi}_{H,t} = \hat{\pi}_t + \hat{\rho}_{H,t} - \hat{\rho}_{H,t-1} \quad (16)$$

$$\hat{\pi}_{H,t}^* = \hat{\pi}_t^* + \hat{\rho}_{H,t}^* - \hat{\rho}_{H,t-1}^* \quad (17)$$

$$\hat{\pi}_{F,t}^* = \hat{\pi}_t^* + \hat{\rho}_{F,t}^* - \hat{\rho}_{F,t-1}^* \quad (18)$$

$$\hat{\pi}_{F,t} = \hat{\pi}_t + \hat{\rho}_{F,t} - \hat{\rho}_{F,t-1} \quad (19)$$

$$(1 - \gamma)\hat{\rho}_{H,t} + \gamma\hat{\rho}_{F,t} = 0 \quad (20)$$

$$(1 - \gamma)\hat{\rho}_{F,t}^* + \gamma\hat{\rho}_{H,t}^* = 0 \quad (21)$$

$$\hat{\rho}_{H,t} = \hat{\rho}_{H,t}^* + \hat{e}_t \quad (22)$$

$$\hat{m}_t^* = \hat{\rho}_{F,t}^* + \hat{e}_t - \hat{\rho}_{F,t} \quad (23)$$

$$\hat{s}_t^* = \hat{\rho}_{H,t} - \hat{\rho}_{F,t} \quad (24)$$

Quadratic loss functions

- Under cooperation:

$$L^W = \frac{1}{2} \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\begin{aligned} & (1 + \omega) (\hat{Y}_t - z_t)^2 + (1 + \omega) (\hat{Y}_t^* - z_t^*)^2 + \Gamma \Sigma^2 \hat{e}_t^2 \\ & + \frac{\varepsilon}{\delta} \left\{ \hat{\pi}_{H,t}^2 + (1 - \gamma) \hat{\pi}_{F,t}^{*2} + \gamma \hat{\pi}_{F,t}^2 \right\} + \Gamma \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right)^2 \\ & + (\sigma - 1) \left\{ \left(\hat{Y}_t + \gamma \Sigma \hat{e}_t + \eta \hat{p}_{H,t} \right)^2 + \left(\hat{Y}_t^* - \gamma \Sigma \hat{e}_t + \eta \gamma \hat{r}_t \right)^2 \right\} \\ & + \eta (1 - \eta) \left\{ (1 - \gamma) \hat{p}_{H,t}^2 + \gamma \hat{p}_{F,t}^2 + (1 - \gamma) \hat{p}_{F,t}^{*2} + \gamma \hat{p}_{H,t}^{*2} \right\} \end{aligned} \right] \\ + \text{t.i.p} + \mathcal{O}(\|\xi_t\|^3), \quad (25)$$

Quadratic loss functions

- Home loss function under noncooperation:

$$L = \frac{1}{2} \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\begin{aligned} & \{1 - \Omega_1(1 + \omega)\} (1 + \omega) \left(\hat{Y}_t - z_t\right)^2 + (1 - \omega\Omega_1) \Gamma \Sigma^2 \hat{e}_t^2 \\ & + \frac{\varepsilon}{\delta} (1 - (1 + \omega)\Omega_1) \hat{\pi}_{H,t}^2 + \frac{\varepsilon}{\delta} \left((1 - \gamma)\omega\Omega_1 - \Omega_3 \right) \hat{\pi}_{F,t}^{*2} \\ & + \gamma \frac{\varepsilon}{\delta} (\omega\Omega_1 + \Omega_2) \hat{\pi}_{F,t}^2 + \Gamma \omega \Omega_1 \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right)^2 \\ & \quad + (\sigma - 1) \left\{ \hat{Y}_t + \gamma \Sigma \hat{e}_t + \eta \hat{p}_{H,t} \right\}^2 \\ & + (1 - \eta) (\eta (1 - \omega\Omega_1) - \Omega_2) \left\{ (1 - \gamma) \hat{p}_{F,t}^{*2} + \gamma \hat{p}_{H,t}^{*2} \right\} \\ & + (1 - \eta) \left(\eta \omega \Omega_1 + \frac{1}{\gamma} \gamma \Omega_2 \right) \left\{ (1 - \gamma) \hat{p}_{H,t}^2 + \gamma \hat{p}_{F,t}^2 \right\} \\ & \quad + \Omega_1 \left\{ (1 - \sigma) \hat{Y}_t - \sigma \gamma \Sigma \hat{e}_t + (1 - \sigma \eta) \hat{p}_{H,t} \right\}^2 \\ & - \Omega_3 \left\{ (\omega + 1) (\hat{Y}_t^* - z_t^*) + \gamma \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right) \right\}^2 \\ & + \Omega_3 \left\{ (1 - \sigma) \left(\hat{Y}_t^* - \gamma \Sigma \hat{e}_t + \eta \gamma \hat{\tau}_t \right) + (1 - \eta) \hat{p}_{F,t}^* \right\}^2 \\ & + \gamma \Omega_2 \left\{ (\omega + 1) (\hat{Y}_t^* - z_t^*) - (1 - \gamma) \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right) \right\}^2 \\ & - \gamma \Omega_2 \left\{ (1 - \sigma) \left(\hat{Y}_t + \gamma \Sigma \hat{e}_t + \eta \hat{p}_{H,t} \right) + (1 - \eta) \hat{p}_{F,t} \right\}^2 \end{aligned} \right] \\ + \text{t.i.p} + \mathcal{O}(\|\xi_t\|^3), \quad (26)$$

Quadratic loss functions

- Foreign loss function under noncooperation:

$$L^* = \frac{1}{2} \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\begin{aligned} & \Omega_1 \left\{ (\omega + 1)(\hat{Y}_t - z_t) \right\}^2 + (1 + \omega) \left(\hat{Y}_t^* - z_t^* \right)^2 + \omega \Omega_1 \Gamma \Sigma^2 \hat{e}_t^2 \\ & + \frac{\varepsilon}{\delta} (1 + \omega) \Omega_1 \hat{\pi}_{H,t}^2 + \frac{\varepsilon}{\delta} (\Omega_3 + (1 - \gamma)(1 - \omega \Omega_1)) \hat{\pi}_{F,t}^2 \\ & \quad + \gamma \frac{\varepsilon}{\delta} ((1 - \omega \Omega_1) - \Omega_2) \hat{\pi}_{F,t}^2 \\ & + \Gamma (1 - \omega \Omega_1) \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right)^2 \\ & \quad + (\sigma - 1) \left\{ \hat{Y}_t^* - \gamma \Sigma \hat{e}_t + \eta \gamma \hat{\tau}_t \right\}^2 \\ & + (1 - \eta) (\Omega_2 + \eta \omega \Omega_1) \left\{ (1 - \gamma) \hat{p}_{F,t}^2 + \gamma \hat{p}_{H,t}^2 \right\} \\ & + (1 - \eta) (\eta (1 - \omega \Omega_1) - \Omega_2) \left\{ (1 - \gamma) \hat{p}_{H,t}^2 + \gamma \hat{p}_{F,t}^2 \right\} \\ & \quad - \Omega_1 \left\{ (1 - \sigma) \hat{Y}_t - \sigma \gamma \Sigma \hat{e}_t + (1 - \sigma \eta) \hat{p}_{H,t} \right\}^2 \\ & + \Omega_3 \left\{ (\omega + 1)(\hat{Y}_t^* - z_t^*) + \gamma \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right) \right\}^2 \\ & - \Omega_3 \left\{ (1 - \sigma) \left(\hat{Y}_t^* - \gamma \Sigma \hat{e}_t + \eta \gamma \hat{\tau}_t \right) + (1 - \eta) \hat{p}_{F,t}^* \right\}^2 \\ & - \gamma \Omega_2 \left\{ (\omega + 1)(\hat{Y}_t^* - z_t^*) - (1 - \gamma) \left(\eta \hat{p}_{F,t} - \frac{\hat{e}_t}{\sigma} - \eta \hat{p}_{F,t}^* \right) \right\}^2 \\ & + \gamma \Omega_2 \left\{ (1 - \sigma) \left(\hat{Y}_t + \gamma \Sigma \hat{e}_t + \eta \hat{p}_{H,t} \right) + (1 - \eta) \hat{p}_{F,t} \right\}^2 \end{aligned} \right] \\ + \text{t.i.p} + \mathcal{O}(\|\xi_t\|^3), \tag{27}$$

Special case

Quadratic **loss functions** in a special case with log utility, unitary elasticity of substitution (Cobb-Douglas aggregate consumption) and no home bias ($\sigma = \eta = 1$ and $\gamma = 0.5$)

$$L = \frac{1}{2} \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\begin{array}{l} \frac{1}{2}(1+\omega) (\hat{Y}_t - z_t)^2 + \frac{1}{2}(1+\omega) (\hat{Y}_t^* - z_t^*)^2 \\ -\frac{\omega+1}{2} (\hat{Y}_t^* - z_t^*) (\hat{p}_{F,t} - \hat{e}_t - \hat{p}_{F,t}^*) \\ + \frac{1}{8} (\hat{p}_{F,t} - \hat{e}_t - \hat{p}_{F,t}^*)^2 + \frac{\varepsilon}{2\delta} \hat{\pi}_{H,t}^2 + \frac{\varepsilon}{2\delta} \hat{\pi}_{F,t}^2 \end{array} \right] + \text{t.i.p} + \mathcal{O}(\|\xi_t\|^3),$$

$$L^* = \frac{1}{2} \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\begin{array}{l} \frac{1}{2}(1+\omega) (\hat{Y}_t - z_t)^2 + \frac{1}{2}(1+\omega) (\hat{Y}_t^* - z_t^*)^2 \\ +\frac{\omega+1}{2} (\hat{Y}_t^* - z_t^*) (\hat{p}_{F,t} - \hat{e}_t - \hat{p}_{F,t}^*) \\ + \frac{1}{8} (\hat{p}_{F,t} - \hat{e}_t - \hat{p}_{F,t}^*)^2 + \frac{\varepsilon}{2\delta} \hat{\pi}_{H,t}^2 + \frac{\varepsilon}{2\delta} \hat{\pi}_{F,t}^2 \end{array} \right] + \text{t.i.p} + \mathcal{O}(\|\xi_t\|^3)$$

$$L^w = \frac{1}{2} \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\begin{array}{l} (1+\omega) (\hat{Y}_t - z_t)^2 + (1+\omega) (\hat{Y}_t^* - z_t^*)^2 \\ + \frac{1}{4} (\hat{p}_{F,t} - \hat{e}_t - \hat{p}_{F,t}^*)^2 + \frac{\varepsilon}{\delta} \hat{\pi}_{H,t}^2 + \frac{\varepsilon}{2\delta} \hat{\pi}_{F,t}^2 + \frac{\varepsilon}{2\delta} \hat{\pi}_{F,t}^2 \end{array} \right] + \text{t.i.p} + \mathcal{O}(\|\xi_t\|^3)$$

Model analysis

Calibration

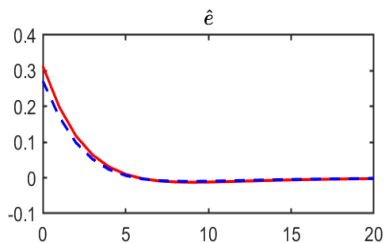
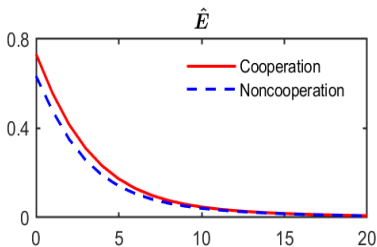
- Parameter values are standard
- Nonetheless, I also use various values of σ , γ and η in computing the gains from cooperation

Table: Parameter values

Parameter	Value	Definition
β	0.99	Discount factor
χ	1	Coefficient associated with labor disutility
ω	4.71	Inverse elasticity of labor supply
σ	3	Degree of risk aversion
θ	0.75	Probability that price cannot be adjusted
η	1.5	Elasticity of substitution between Home and Foreign goods
γ	0.5	Weight of imported goods in consumption basket

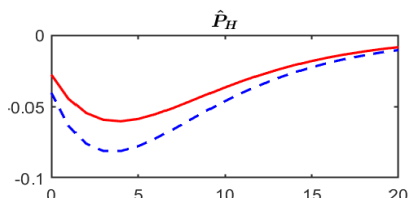
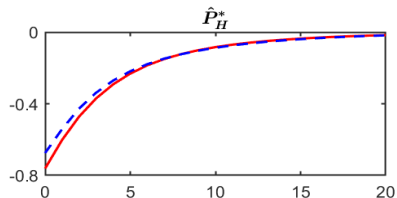
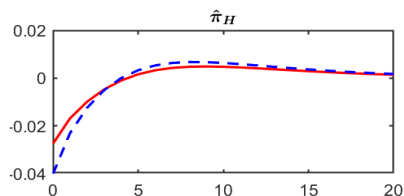
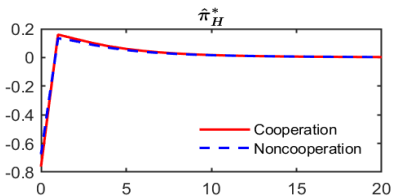
Impulse responses

- Responses of several variables in the DP model under cooperation and noncooperation to a positive one standard deviation productivity shock
- Under noncooperation, nominal exchange rate E depreciates by less than under cooperation, and thus real exchange rate e also depreciates by less



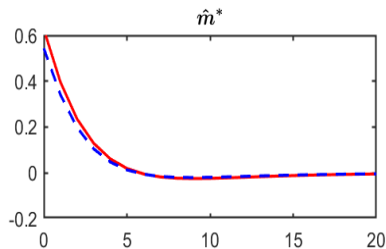
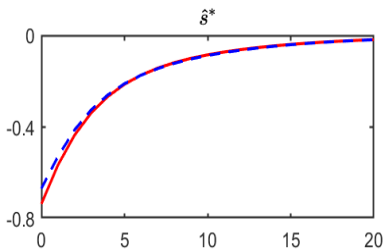
Impulse responses

- Hence, P_H^* falls by less and P_H falls by more \rightarrow a smaller decline in π_H^* and a larger fall in π_H



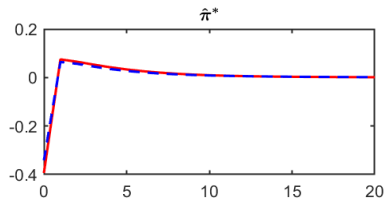
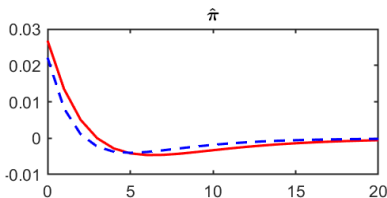
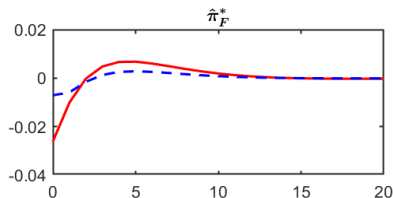
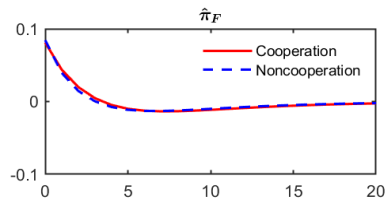
Impulse responses

- Accordingly, s^* decreases by less and m^* rise by less



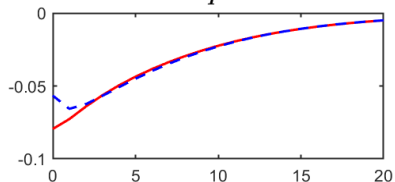
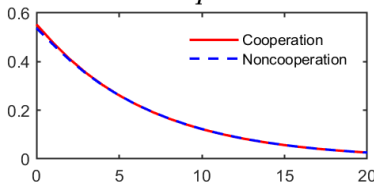
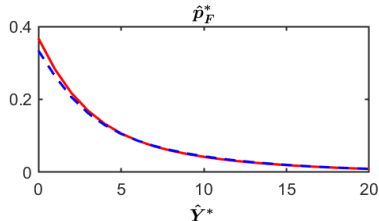
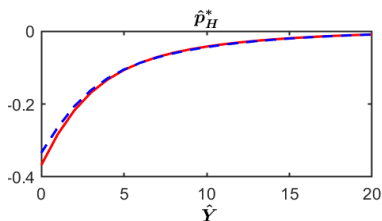
Impulse responses

- From NKPCs, a smaller decrease in π_F^* and a slightly greater rise in π_F
- As a result, π increases by less and π^* drops by less



Impulse responses

- Smaller increase in p_F^* \rightarrow smaller fall in Y^*
- Smaller decrease in p_H^* \rightarrow Y increases by less



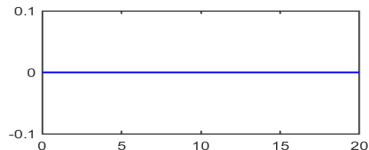
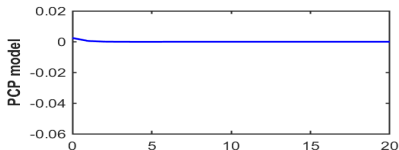
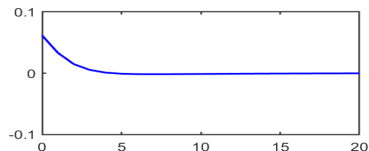
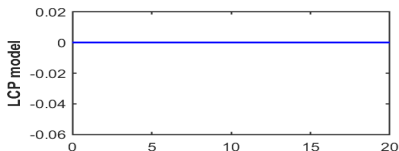
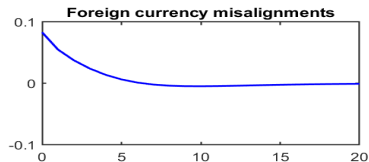
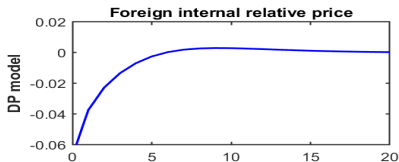
Impulse responses

- Optimal monetary policy under noncooperation produces more stable Home CPI inflation π but more volatile Home PPI inflation π_H and import price inflation π_F
- On the other hand, in Foreign, more stable CPI inflation π^* , PPI inflation π_F^* and import price inflation π_H^* are generated by optimal monetary policy under noncooperation
- And, Home output Y increases by less and Foreign output Y^* falls by less compared to those under cooperation.

Difference between impulse responses

- In the DP model, there are inefficiencies arising from both internal relative price and currency misalignments
- ⇒ Responses of internal relative price and currency misalignments under cooperation and noncooperation are different
- In the LCP model, there is no inefficiency stemming from internal relative price
- ⇒ Responses of currency misalignments under cooperation and noncooperation are different
- In the PCP model, there is no inefficiency stemming from currency misalignments
- ⇒ Responses of internal relative price under cooperation and noncooperation are different

Difference between impulse responses



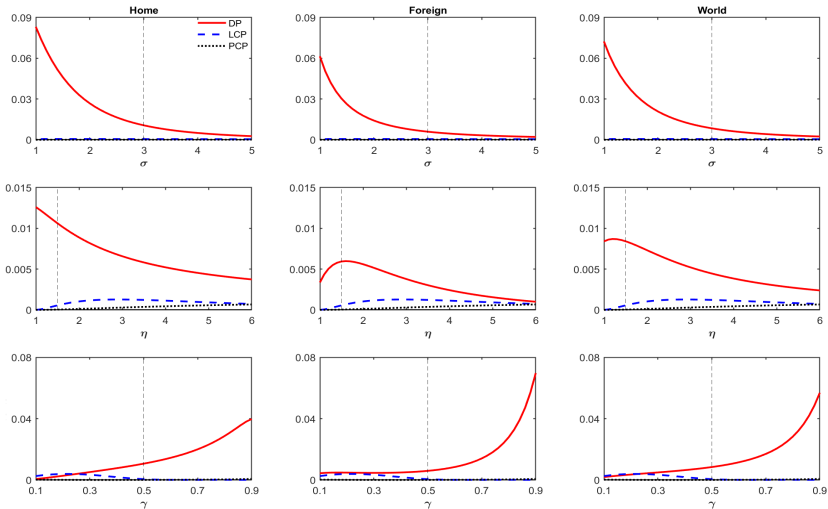
Welfare costs

- Consumption units by Lucas (1992) are used in computing the welfare costs.
- Welfare costs are aggregate consumption that a representative household has to give up to be as well off under cooperation as under noncooperation
- Let λ^C be the welfare cost from noncooperation of the Home representative household

$$W_H^N = \mathbb{E}_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left[\frac{\{(1 - \lambda^C) C_t^C\}^{1-\sigma}}{1 - \sigma} - \chi \frac{h_t^{C^{1+\omega}}}{1 + \omega} \right]$$

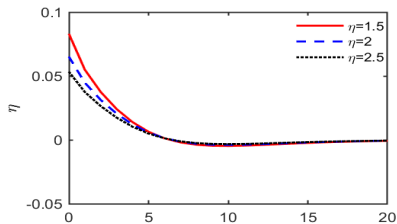
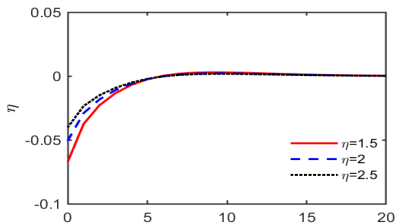
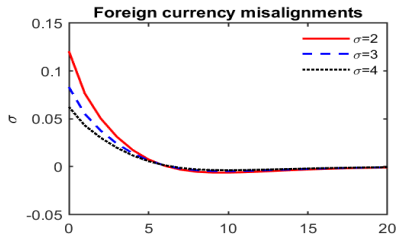
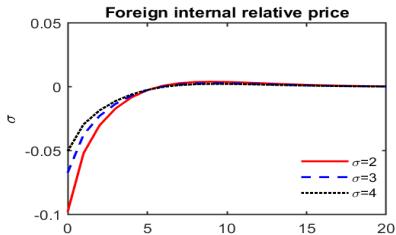
Welfare costs

Welfare gains



Welfare costs

Welfare costs



Conclusion

Conclusion

- This paper considers **optimal monetary policy in a two-country model under DP**
- In the DP model, there is **one more inefficiency** than in the LCP and PCP models
 - Internal relative price distortion compared to the LCP model, and distortion arising from deviations from the law of one price compared to the PCP model
- Accordingly, **welfare gains** from monetary policy cooperation in the DP model are substantially **greater** than in the LCP and PCP models

Conclusion

- Moreover, **noncooperative Foreign policymaker** in the DP model **can manipulate** not only **internal relative price** but also **deviations from LOOP** in favor of its own welfare through nominal exchange rate adjustment
- While **noncooperative Home policymaker** can **control neither** of the two
- Thus, **gains from cooperation in Home are larger** compared to Foreign

Conclusion

- This result also **rationalizes** the fact that the **U.S. designates currency manipulators** to protect its welfare
- Furthermore, I find that there are substantial **gains from cooperation in the DP model even under the conditions** that make **gains from cooperation in the LCP and PCP models disappear**

Thank you

Thank you